The basics of statistical testing

23/11/2021

dplyr and data wrangling

Function	Effect		
select()	Include or exclude variables (columns)		
arrange()	Change the order of observations (rows)		
filter()	Include or exclude observations (rows)		
mutate()	Create new variables (columns)		
group_by()	Create groups of observations		
summarise()	Aggregate or summarise groups of observations (rows)		

Importing, transforming, and summarising your data

library(readr)
crime <- read_csv("data/crime.csv")
crime</pre>

##	# A	A tibble: 301 >	< 15									
##		Participant	sex	age	victim_crime	Н	E	Х	А	С	0	SA
##		<chr></chr>	<chr> <c< td=""><td>dbl></td><td><chr></chr></td><td><dbl></dbl></td><td><dbl></dbl></td><td><dbl></dbl></td><td><dbl></dbl></td><td><dbl></dbl></td><td><dbl></dbl></td><td><dbl></dbl></td></c<></chr>	dbl>	<chr></chr>	<dbl></dbl>						
##	1	R_01TjXgC191~	male	55	yes	3.7	3	3.4	3.9	3.2	3.6	1.15
##	2	R_0dN5YeULcy~	fema~	20	no	2.5	3.1	2.5	2.4	2.2	3.1	2.05
##	3	R_0DPiPYWhnc~	male	57	yes	2.6	3.1	3.3	3.1	4.3	2.8	2
##	4	R_0f7bSsH6Up~	male	19	no	3.5	1.8	3.3	3.4	2.1	2.7	1.55
##	5	R_0rov2RoSkP~	fema~	20	no	3.3	3.4	3.9	3.2	2.8	3.9	1.3
##	6	R_0wioqGERxE~	fema~	20	no	2.6	2.6	3	2.6	2.9	3.4	2.55
##	7	R_0wR08lNe0k~	male	34	yes	3.2	2.5	3.2	2.8	4	3.2	1.85
##	8	R_116nEdFsGD~	fema~	19	no	2.9	4	3.9	4.2	3.7	1.9	1.1
##	9	R_11ZmBd5VEk~	fema~	19	yes	3.4	3.4	3.3	3.4	3.2	3.2	2.2
##	10	R_12i26Qzosm~	male	20	no	2.4	2.1	1.8	2.2	3.4	2.9	2.15

Importing, transforming, and summarising your data

A tibble: 2 x 4
Sex mean_pop median_pop max_population
<chr> <dbl> <dbl> <dbl> <dbl>
1 Female 184. 98 536
2 Male 513. 462. 2082

Importing, transforming, and summarising your data

```
grouped_crime <- group_by(crime, sex, victim_crime)
summarise(grouped_crime,
    state_anxiety = mean(SA),
    sd_SA = sd(SA),
    var SA = var(SA))</pre>
```

```
## # A tibble: 4 x 5
## # Groups: sex [2]
  sex victim_crime state_anxiety sd_SA var_SA
##
##
   <chr> <chr>
                              <dbl> <dbl> <dbl>
## 1 female no
                              1.90 0.518 0.268
## 2 female yes
                             1.98 0.643 0.413
## 3 male
                               2.02 0.553 0.306
         no
## 4 male yes
                            1.74 0.472 0.223
```

Things we've covered

- 1. How to structure data through data.frames
- 2. How to handle different types of data (characters, numbers, logicals)
- 3. How to import different types of data
- 4. How to visualize your data
- 5. How to select only the data you need
- 6. How to summarise data

You've come a long way!



Some R (and beyond) tips



The Practical Developer @ThePracticalDev



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Google Search

I'm Feeling Lucky



Introducing Google Home Hub. Now in stock.

Some notes about Discovering Statistics Using R



- 1. Great as a *reference* book for stats. If you want to know more about the underlying maths or rationale of a given test, you'll find it in here.
- 2. If you don't know how to do a particular test, or what test you need, find it in here.
- 3. The coding style I've taught you differs. Both styles are fine.
- 4. There is no need to read it cover to cover.

Don't despair: be patient!



Hadley Wickham < @hadleywickham

Just spent 5 minutes staring at this code trying to figure out what was wrong 😬

all_units <- c(setNames(powers, pa setNames(powers. pa (\mathbf{i}) 6:03 PM · Oct 27, 2019 ♡ 1.4K Q 114 S Copy link to Tweet **Tweet your reply**

Basic Research Design and Null Hypothesis Significance Testing

Research questions

In research, you typically start with a question:

- Do people find object recognition easier if the picture is in colour or in black and white?
- Is the blue pill or red pill better for treating a cold?
- Are people who have been a victim of crime more afraid of crime?

How do we measure the phenomena we talk about and compare them across groups of people?

Operationalizing your variables

We don't typically have direct access to the *underlying*, *psychological* phenomena. Thus, we need to work how to measure them.

For example, Ellis & Renouf (2018) used questionnaires to assess people's personality traits and fear of crime.

head(select(crime, H:O), 6)								head(select(crime, FoC, Foc2), 6)
##	#	A tibb	ole: 6	x 6				## # A tibble: 6 x 2
##		Н	Е	Х	А	С	0	## FoC Foc2
##		<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	## <dbl> <dbl></dbl></dbl>
##	1	3.7	3	3.4	3.9	3.2	3.6	## 1 2.6 3
##	2	2.5	3.1	2.5	2.4	2.2	3.1	## 2 2 3
##	3	2.6	3.1	3.3	3.1	4.3	2.8	## 3 1.2 2
##	4	3.5	1.8	3.3	3.4	2.1	2.7	## 4 3.2 5
##	5	3.3	3.4	3.9	3.2	2.8	3.9	## 5 2.8 3
##	6	2.6	2.6	3	2.6	2.9	3.4	## 6 2 4

The Fear of Crime dataset

Some of the fundamental research questions for the Fear of Crime experiment Ellis & Renouf (2018) were:

- 1. Do men and women differ in terms of their fear of crime?
- 2. Are people who have been a victim of crime more fearful of crime?

select(crime, sex, victim_crime, FoC)

##	# /	A tibble	e: 301 x 3	
##		sex	victim_crime	FoC
##		<chr></chr>	<chr></chr>	<dbl></dbl>
##	1	male	yes	2.6
##	2	female	no	2
##	3	male	yes	1.2
##	4	male	no	3.2
##	5	female	no	2.8
##	6	female	no	2
##	7	male	yes	1.6
##	8	female	no	2
##	9	female	yes	3.4
##	10	male	no	1.4
##	#	with	n 291 more row	VS

Null Hypothesis Significance Testing (NHST)

Null Hypothesis Significance Testing is a statistical framework for answering these types of questions.

Our *hypothesis* is that people who have been a victim of crime will be more afraid of it, so we ask:

• "Are people who have been a victim of crime more fearful of crime?"

What we test is how likely it would be to get the data we have *if the null hypothesis were true*:

 If people who have not been a victim of crime are as fearful of crime as people who have, how likely are the results we have obtained?

The *t*-test family

The statistical test of choice for comparing two groups is the two sample *t*-test.

- 1. Independent t-tests
 - Compare means across different groups (e.g. groups of people)
 - Also called between-subjects
- 2. Paired t-tests
 - Compares means across related data (e.g. data from the same people measured twice)
 - Also called repeated-measures

We use the t.test() function for all of these!



Independent samples

Let's test whether the mean Fear of Crime differs between victims of crime and non-victims.

Victims and non-victims are two independent groups, so we need an independent (or two-sample t-test).

```
##
## Welch Two Sample t-test
##
## data: FoC by victim_crime
## t = 0.45309, df = 197.48, p-value = 0.651
## alternative hypothesis: true difference in means between group no and group yes is not equal to 6
## 95 percent confidence interval:
## -0.1873001 0.2990388
## sample estimates:
## mean in group no mean in group yes
## 2.463636 2.407767
```

The tilde (~) symbol in R usually means "modelled by". The dependent variable goes before "~".

```
FoC ~ victim_crime means FoC modelled by victim_crime.
```

data = crime tells R to look in the crime data
frame for the data.

paired = FALSE tells R that this is an independent
samples test.

```
##
## Welch Two Sample t-test
##
## data: FoC by victim_crime
## t = 0.45309, df = 197.48, p-value = 0.651
## alternative hypothesis: true difference in means
## 95 percent confidence interval:
## -0.1873001 0.2990388
## sample estimates:
## mean in group no mean in group yes
## 2.463636 2.407767
```

The output shows the key statistics in oneline:

"t = 0.453, df = 197.479, p-value = 0.651"

A p-value is the probability of obtaining this difference between means if the null hypothesis is true.

Conventionally, we consider a p-value < .05 to be *significant*, allowing us to *reject* the null hypothesis.

```
##
      Welch Two Sample t-test
##
##
## data: FoC by victim_crime
## t = 0.45309, df = 197.48, p-value = 0.651
## alternative hypothesis: true difference in means
  95 percent confidence interval:
##
   -0.1873001 0.2990388
##
## sample estimates:
   mean in group no mean in group yes
##
##
            2.463636
                              2.407767
```

There are also *sample estimates*, i.e. the group means, and confidence intervals of the *difference* between means.

Confidence intervals are a measure of *uncertainty*; the broader they are, the more uncertain about the accuracy of the values we have estimated.

Here, they overlap zero; the data is compatible with both negative and positive differences in fear of crime.

##		
##	Welch Two Sample t-test	
##		
##	data: FoC by victim_crime	
##	t = 0.45309, df = 197.48, p-value = 0.651	
##	alternative hypothesis: true difference in	means
##	95 percent confidence interval:	
##	-0.1873001 0.2990388	
##	sample estimates:	
##	mean in group no mean in group yes	
##	2.463636 2.407767	

Visualizing the results

Here I plot a representation of the results using ggplot()

stat_summary() can be used to calculate
and plot summary statistics.

By default, it calculates the *mean and standard error of the mean (SEM)*.

The SEM is another measure of uncertainty, providing a measure of how *accurately* we've estimated the mean.

ggplot(crime, aes(x = victim_crime, y = FoC
 stat_summary(fun.data = mean_se) +
 theme_classic()



Descriptive statistics

We can also calculate these summary statistics directly.

The SEM is the *standard deviation* divided by the *square root* - sqrt() - of the sample size.

$$\sigma^M = rac{\sigma}{\sqrt(N)}$$

crime %>%
group_by(victim_crime) %>%
summarise(n = n(),
 mu = mean(FoC),
 std = sd(FoC),
 sem = std/sqrt(n))

##	#	A tibble: 2 >	< 5			
##		victim_crime	n	mu	std	sem
##		<chr></chr>	<int></int>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>
##	1	no	198	2.46	0.980	0.0696
##	2	yes	103	2.41	1.03	0.102

Paired samples

None of the measures in the crime dataset are *repeated* or *paired*, so for a moment we need to switch to another dataset.

crossmod is a dataset from a cognitive experiment in which participants identified objects using by touch. They did this twice. Sometimes the objects changed size; sometimes they stayed the same. The hypothesis was that changing size would slow down naming. crossmod <- read_csv("data/crossmod.csv")
crossmod</pre>

##	#	А	t	ibble	::	48	Х	3				
##		p	bai	rtici	pa	ant	S	ize			RT	
##				<	dł	ol>	< (chr	>	<db< td=""><td>l></td><td></td></db<>	l>	
##	1					1	DS	S	•	260	8.	
##	2					1	SS	S	•	219	5	
##	3					2	DS	S	•	255	1	
##	4					2	SS	5	•	221	3	
##	5					3	DS	5	•	290	0.	
##	6					3	SS	5	•	278	8.	
##	7					4	DS	5	•	264	6.	
##	8					4	SS	5	•	239	0.	
##	9					5	DS	5		348	6.	
##	10					5	SS	5		284	4.	
##	#		•	with	1 3	38	mon	re	ro	NS		

Since the data contains repeated measurements from the same participants, we need to run a paired/repeatedmeasures t-test. So we simply change paired = FALSE to paired = TRUE!

t.test(RT ~ Size, data = crossmod, paired = TRUE)

```
##
## Paired t-test
##
## data: RT by Size
## t = 3.512, df = 23, p-value = 0.001872
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 99.91035 386.29799
## sample estimates:
## mean of the differences
## 243.1042
```

This time, there was a significant difference!

Checking assumptions

Assumptions of the *t*-test

Before we get too carried away with our results, we have to check our assumptions!

- 1. The dependent variable must be continuous (and *interval* or *ratio*).
- 2. The independent variable must be categorical.
- 3. The distribution of the data should be approximately normal.

Independent t-tests have a couple of extra assumptions:

1. The data in each sample should be *independent* (i.e. come from different people)

2. The variance of the data in each group should be the same (*Homogeneity of variance*).

	RESULT - EINAL	
	1 JAM VISAIN BOLT	9.63
Stat A	2 JAM YOHAN BLAKE	9.75
	3 USA JUSTIN GATLIN	9.79
	4 USA TYSON GAY	9.80
	5 USA RYAN BAILEY	9.88
A Section (6 NED CHURANDY MARTINA	9.94
	7 TRI KI RICHARD THOMPSON	9.98
Service of all	8 JAM ASAFA POWELL	11.99
O BBC		

Nominal data

Nominal data is categorical data that has no natural order.

For example, the runners' names (e.g. Usain Bolt, Asafa Powell, Tyson Gay) and nationalities (e.g. Jamaica, USA) are **nominal**.

	Ŕ	Men's 100m	9989
2	n	RESULT - FINAL	₩IND +1.5M/S
1	JAM 🚬	🗲 USAIN BOLT	<u>OR</u> 9.63
2	JAM 🚬	🗲 YOHAN BLAKE	9.75
3	USA-	JUSTIN GATLIN	9.79
4	USA-	TYSON GAY	9.80
5	USA	RYAN BAILEY	9.88
6	NED	CHURANDY MARTINA	9.94
7	TRI	RICHARD THOMPSON	9.98
8	JAM	🗲 🗛 ASAFA POWELL	11.99

Ordinal data

Ordinal data is also categorical, but is *ordered*. The gaps between the categories are not necessarily equal.

e.g. finishing position is ordinal, but the gap between first and second is bigger than the gap between second and third!

	Ŕ	Men's 100m	696
1	m	RESULT - FINAL	🔧 Wind +1.5m/s
1	JAM.🔀	🗲 USAIN BOLT	9.63
2	JAM.🔀	YOHAN BLAKE	9.75
3	USA	JUSTIN GATLIN	9.79
4	USA	TYSON GAY	9.80
5	USA	RYAN BAILEY	9.88
6	NED	CHURANDY MARTINA	9.94
7	TRI	RICHARD THOMPSON	9.98
8	JAM.	ASAFA POWELL	11.99

Interval data

Interval data is data with equally spaced intervals. (e.g. the gap between 9 seconds and 10 seconds is the same as the gap between 12 seconds and 13 seconds)

MEN'S 100M RESULT - FINAL WIND +1.5M/S USAIN BOLT OR 9.63 JAM> JAM YOHAN BLAKE 9.75 JUSTIN GATLIN 9.79 USA TYSON GAY 9.80 USA RYAN BAILEY 9.88 USA CHURANDY MARTINA 9.94 NFD-**RICHARD THOMPSON** 9.98 ASAFA POWELL 11.99

Ratio data

Ratio data is similar to interval data, but has a meaningful boundary at zero (e.g. a finishing time cannot be below zero.)

The assumption of normality



The assumption of normality

A normal distribution can be easily described by two parameters: the mean - μ - and the standard deviation - σ .

The normal distribution is symmetrical.

For example, Mean Intelligence Quotient is 100; the standard deviation is 15. Thus, it's easy to draw what the distribution of IQ should look like.



Checking normality

Plotting our data is a simple way to check normality!

Our data are clearly *skewed* - more values are to the left than to the right.

If you need to test normality formally, use the Shapiro-Wilks test - **shapiro.test()**.



Checking normality

With a repeated-measures design, we care about the normality of the *differences* between pairs.

```
crossmod_wide <-
  crossmod %>%
  spread(Size, RT) %>%
  mutate(size_diff = DS - SS)
```



Checking normality

This looks a little suspicious. There's probably an *outlier* at the far right side of the plot (more on these next session).

shapiro.test(crossmod_wide\$size_diff)

```
##
## Shapiro-Wilk normality test
##
## data: crossmod_wide$size_diff
## W = 0.83796, p-value = 0.001318
```

The Shapiro-Wilks test is significant, suggesting that normality is violated.



Remember how a normal distribution can be described by two parameters: the mean and the standard deviation.

As we change the mean, the distribution moves along the x-axis.

With a *t*-test we only want to pick up differences in the location of the *means* along the x-axis representing our dependent variable.



Our ability to detect differences in the location of the means is hampered if the *standard deviation* (or the *variance*, which is sd^2) differs across groups.

As the standard deviation increases, the variability around the mean increases, and the distribution of values gets *broader*.

Here, I doubled the standard deviation of the second distribution to 30.

Differences in variance across groups can *bias* your statistics in complex ways.



Let's look again at our distributions for Fear of Crime.

Although they're skewed, it looks like they're similarly variable.

We can test this statistically using Levene's test from the **car** package:

library(car)
leveneTest(FoC ~ victim_crime, data = crime

Levene's Test for Homogeneity of Variance (center = median)
Df F value Pr(>F)
group 1 0.3669 0.5451
299

It's not significant, consistent with our visual impressions.



The assumption of independence

From the crossmod dataset, RTs across the two conditions have a strong positive relationship.

Values generated by the same people on repeated occasions tend to be correlated.

This one is easy to assess: we know from the design whether the data is independent or not! ## `geom_smooth()` using formula 'y ~ x'



What to do about violated assumptions

What to do about violated assumptions

- 1. When homogeneity of variance is violated
 - Welch's t-test does not assume equality/homogeneity of variance. By default, R uses Welch's t-test for independent samples.
 - This is only a problem for independent samples t-tests.
- 2. When independence is violated
 - Use a paired/repeated-measures t-test.
- 3. When normality is violated
 - Often...nothing is done, or the data is *transformed* (we'll cover that in detail next term).
 - Consider non-parametric tests

Non-parametric t-tests

Consider using non-parametric statistics, which make fewer assumptions.

The most frequently used tests are the Wilcoxon rank-sum test (sometimes called the Mann-Whitney U test) for independent samples data, and the Wilcoxon signed-rank test for paired samples data.

```
Simply substitute t.test() for wilcox.test()!
```

wilcox.test(FoC ~ victim_crime, data = crime, paired = FALSE)

```
##
## Wilcoxon rank sum test with continuity correction
##
## data: FoC by victim_crime
## W = 10623, p-value = 0.5517
## alternative hypothesis: true location shift is not equal to 0
```

Reporting the results of a t-test

```
t.test(FoC ~ victim_crime, data = crime)
                                               crime %>%
                                                 group_by(victim_crime) %>%
                                                 summarise(means = mean(FoC),
##
                                                          sem = sd(FoC) / sqrt(n()))
##
      Welch Two Sample t-test
##
                                            ## # A tibble: 2 x 3
## data: FoC by victim_crime
## t = 0.45309, df = 197.48, p-value = 0.651  ## victim_crime means
                                                                       sem
## alternative hypothesis: true difference in mea## between group nodend grdbp>yes is not equal to @
## 95 percent confidence interval:
                                           ## 1 no 2.46 0.0696
## -0.1873001 0.2990388
                                              ## 2 yes 2.41 0.102
## sample estimates:
## mean in group no mean in group yes
##
           2.463636
                           2.407767
```

Reporting the results of a *t*-test

"On average, participants who had been victims of crime did not have significantly higher Fear of Crime (M = 2.41, SE = .10) than participants who had not (M = 2.46, SE = .07), t(197.48) = .453, p = .7."

Means and standard errors are typically reported to two decimal places.

t-values are usually reported to three decimal places.

Exact *p*-values should be reported down to three decimal places; if the p-value is below .001, report "*p* < .001".

Remember to specify, *somewhere*, what type of *t*-test you used.

(for further guidance, see Field et al, Discovering statistics using R)

A plotting suggestion

One way to compare distributions is graphically.

Here we plot the data from each sample using boxplots, with individual data overlaid as points.

Each point is the score for an individual.

```
crime %>%
ggplot(aes(x = victim_crime, y = FoC)) +
geom_jitter(width = 0.05, alpha = 0.5) +
geom_boxplot(alpha = 0.5) +
theme_classic() +
labs(y = "Fear of crime", x = "Victim of
```



Next session

Next week we'll look into **regression** and **correlation**.

Chapters 6 (Correlation) and 7 (Regression) of Discovering Statistics Using R.

Reminder - don't feel you have to read every word!

Look at the introductory sections of each chapter, refer back to the rest *as necessary*.